

# Accelerating Dynamic Graph Analytics on GPUs

Mo Sha<sup>†</sup>, Yuchen Li<sup>‡</sup>, Bingsheng He<sup>†</sup>, Kian-Lee Tan<sup>†</sup>

<sup>†</sup>School of Computing, National University of Singapore

<sup>‡</sup>School of Information Systems, Singapore Management University

Presenter: Mo Sha

Aug 29<sup>th</sup>, 2018



# Outline

- **Introduction**
- **GPMA Dynamic Graph Processing**
- **GPMA+ Optimization**
- **Evaluation**
- **Conclusion**

# Introduction

## *GPU Accelerated Graph Analytics*



[1] <https://gunrock.github.io>

[2] <https://developer.nvidia.com/nvgraph>

[3] <https://github.com/pymedusa/Medusa>

# Introduction

## *GPU Accelerated Graph Analytics*

- Existing GPU Accelerated Graph Analytics focus on conducting graph primitives on static graphs.
- CSR(-like) graph format is widely used due to GPU computational architecture for better parallelism scheduling.

Sparse Matrix

|    |   |   |   |    |
|----|---|---|---|----|
| 10 | 0 | 0 | 0 | -2 |
| 3  | 9 | 0 | 0 | 0  |
| 0  | 7 | 8 | 7 | 0  |
| 3  | 0 | 8 | 7 | 5  |
| 0  | 8 | 0 | 9 | 13 |

Row pointer array

|   |   |   |   |    |    |
|---|---|---|---|----|----|
| 0 | 2 | 4 | 7 | 11 | 14 |
|---|---|---|---|----|----|

Column indices array

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 0 | 4 | 0 | 1 | 1 | 2 | 3 | 0 | 2 | 3 | 4 | 1 | 3 | 4 |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Values array

|    |    |   |   |   |   |   |   |   |   |   |   |   |    |
|----|----|---|---|---|---|---|---|---|---|---|---|---|----|
| 10 | -2 | 3 | 9 | 7 | 8 | 7 | 3 | 8 | 7 | 5 | 8 | 9 | 13 |
|----|----|---|---|---|---|---|---|---|---|---|---|---|----|

# Introduction

## *GPU Accelerated Graph Analytics*

- Existing GPU Accelerated Graph Analytics focus on conducting graph primitives on static graphs.
- CSR(-like) graph format is widely used due to GPU computational architecture for better parallelism scheduling.
- For evolving graphs, an entire rebuilding is required for each single update, which significantly limits the performance on evolving graphs.

# Introduction

## *Dynamic Graph Format on GPUs requires ...*

- To support edge insertion, deletion, and edge value modification.
- To be compatible with existing GPU-based graph algorithms.
- An acceptable trade-off between update efficiency and the overhead introduced.

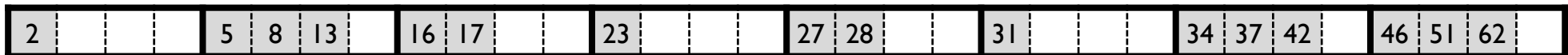
# Outline

- Introduction
- **GPMA Dynamic Graph Processing**
- **GPMA+ Optimization**
- Evaluation
- Conclusion

# GPMA Dynamic Graph Processing

## Introduce **Packed Memory Array** into **GPU Graph Analytics**

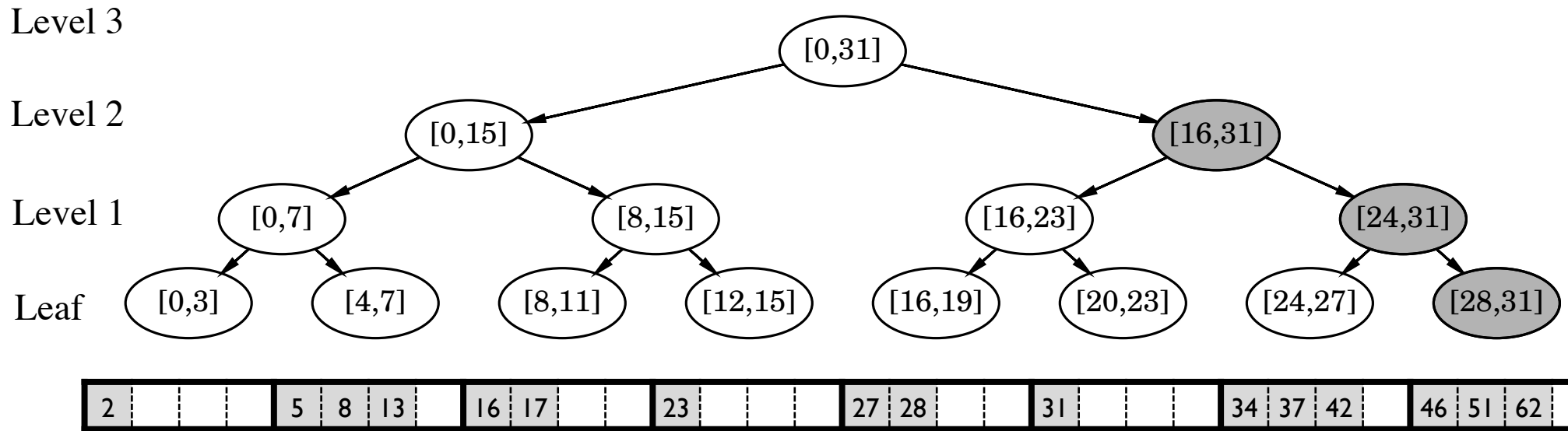
- Sort elements in a partially continuous fashion
- Leave gaps on each segment with a bounded ratio
- Self-balancing binary tree structure
- The amortized insertion complexity of PMA is proved to be  $O(\log^2 N)$  in the worst case and  $O(\log N)$  in the average case.





# GPMA Dynamic Graph Processing

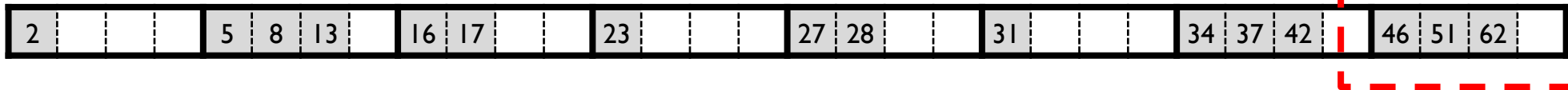
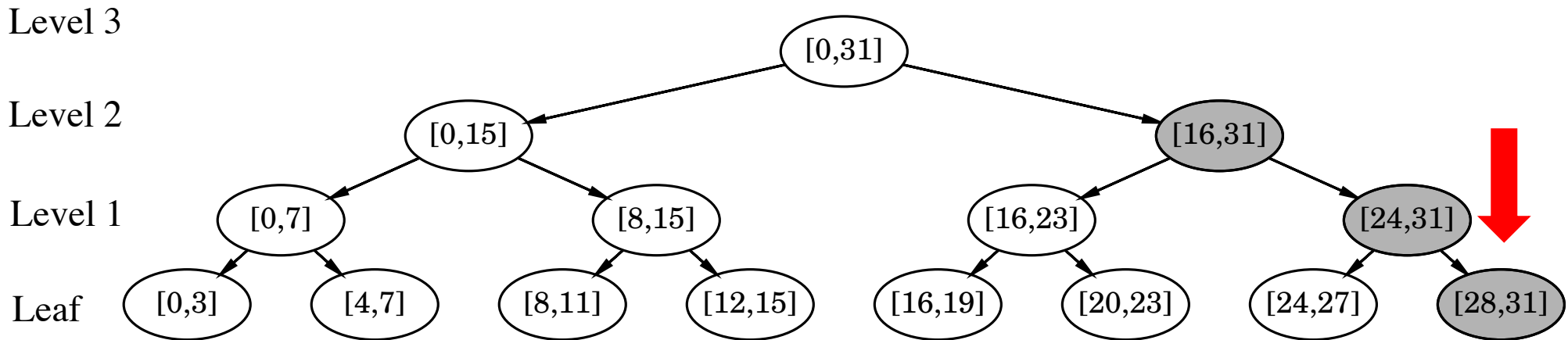
|                            | Leaf | Level 1 | Level 2 | Level 3 |
|----------------------------|------|---------|---------|---------|
| segment size               | 4    | 8       | 16      | 32      |
| density lower bound $\rho$ | 0.08 | 0.19    | 0.29    | 0.40    |
| density upper bound $\tau$ | 0.92 | 0.88    | 0.84    | 0.80    |
| min # of entries           | 1    | 2       | 4       | 8       |
| max # of entries           | 3    | 6       | 12      | 24      |



- [1] Bender, M. A., Demaine, E. D., & Farach-Colton, M. Cache-oblivious b-trees. *SIAM J. Comput.*, 35(2):341–358, 2005.
- [2] M. A. Bender and H. Hu. An adaptive packed-memory array. *ACM Trans. Database Syst.*, 32(4), 2007.

# GPMA Dynamic Graph Processing

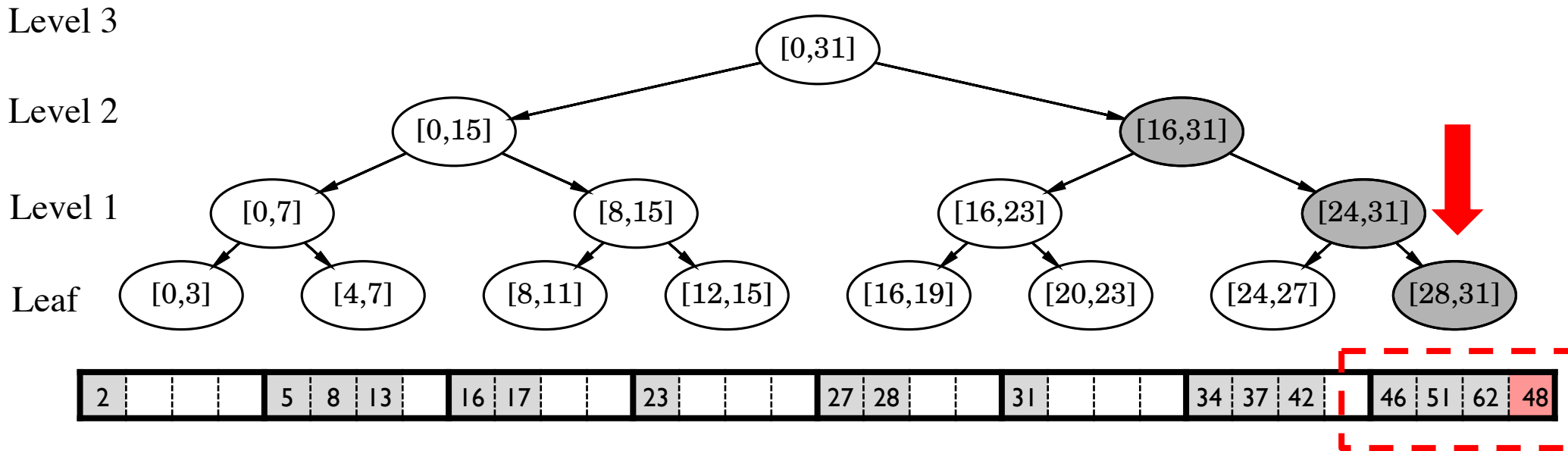
|                            | Leaf | Level 1 | Level 2 | Level 3 |
|----------------------------|------|---------|---------|---------|
| segment size               | 4    | 8       | 16      | 32      |
| density lower bound $\rho$ | 0.08 | 0.19    | 0.29    | 0.40    |
| density upper bound $\tau$ | 0.92 | 0.88    | 0.84    | 0.80    |
| min # of entries           | 1    | 2       | 4       | 8       |
| max # of entries           | 3    | 6       | 12      | 24      |



[1] Bender, M. A., Demaine, E. D., & Farach-Colton, M. Cache-oblivious b-trees. *SIAM J. Comput.*, 35(2):341–358, 2005.  
 [2] M. A. Bender and H. Hu. An adaptive packed-memory array. *ACM Trans. Database Syst.*, 32(4), 2007.

# GPMA Dynamic Graph Processing

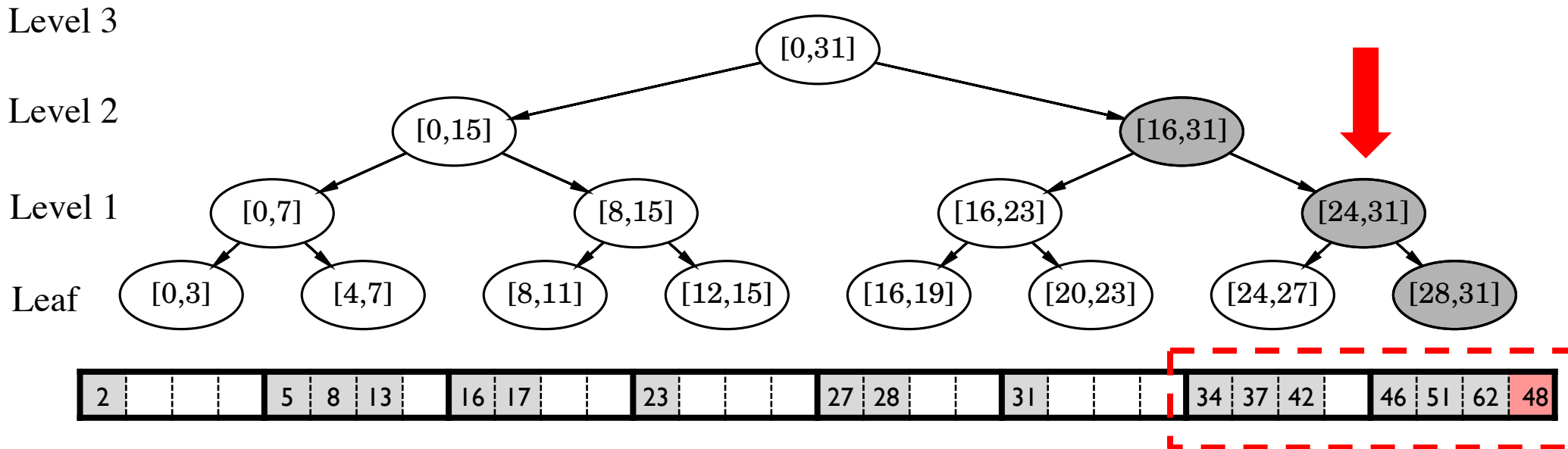
|                            | Leaf | Level 1 | Level 2 | Level 3 |
|----------------------------|------|---------|---------|---------|
| segment size               | 4    | 8       | 16      | 32      |
| density lower bound $\rho$ | 0.08 | 0.19    | 0.29    | 0.40    |
| density upper bound $\tau$ | 0.92 | 0.88    | 0.84    | 0.80    |
| min # of entries           | 1    | 2       | 4       | 8       |
| max # of entries           | 3    | 6       | 12      | 24      |



[1] Bender, M. A., Demaine, E. D., & Farach-Colton, M. Cache-oblivious b-trees. *SIAM J. Comput.*, 35(2):341–358, 2005.  
 [2] M. A. Bender and H. Hu. An adaptive packed-memory array. *ACM Trans. Database Syst.*, 32(4), 2007.

# GPMA Dynamic Graph Processing

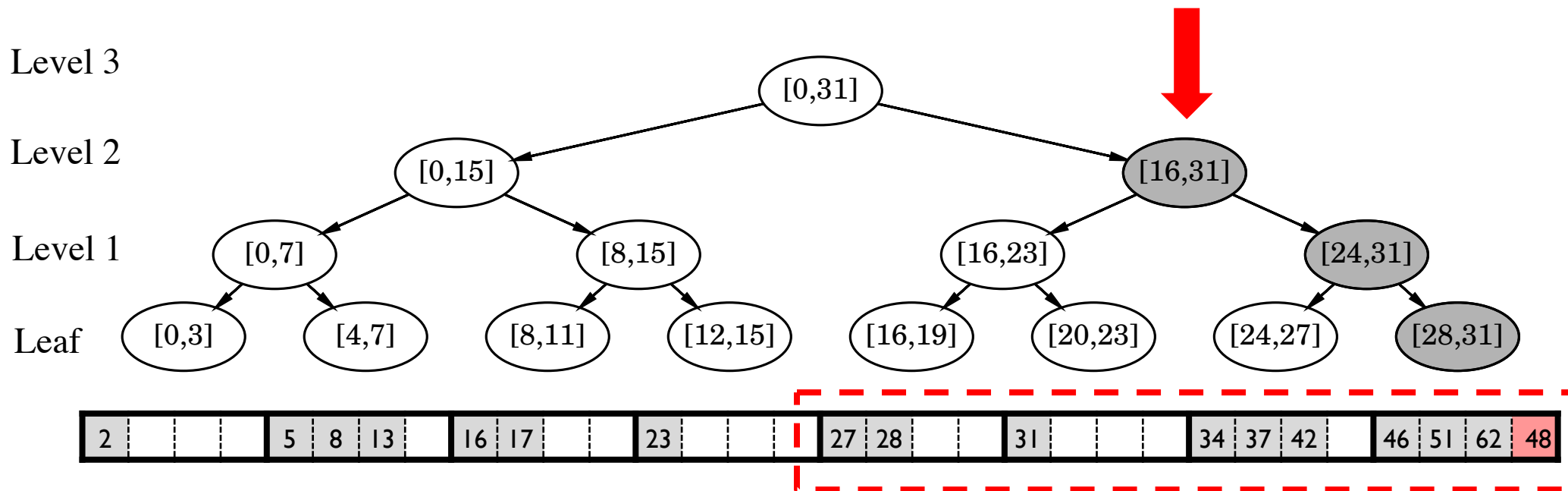
|                            | Leaf | Level 1 | Level 2 | Level 3 |
|----------------------------|------|---------|---------|---------|
| segment size               | 4    | 8       | 16      | 32      |
| density lower bound $\rho$ | 0.08 | 0.19    | 0.29    | 0.40    |
| density upper bound $\tau$ | 0.92 | 0.88    | 0.84    | 0.80    |
| min # of entries           | 1    | 2       | 4       | 8       |
| max # of entries           | 3    | 6       | 12      | 24      |



[1] Bender, M. A., Demaine, E. D., & Farach-Colton, M. Cache-oblivious b-trees. *SIAM J. Comput.*, 35(2):341–358, 2005.  
 [2] M. A. Bender and H. Hu. An adaptive packed-memory array. *ACM Trans. Database Syst.*, 32(4), 2007.

# GPMA Dynamic Graph Processing

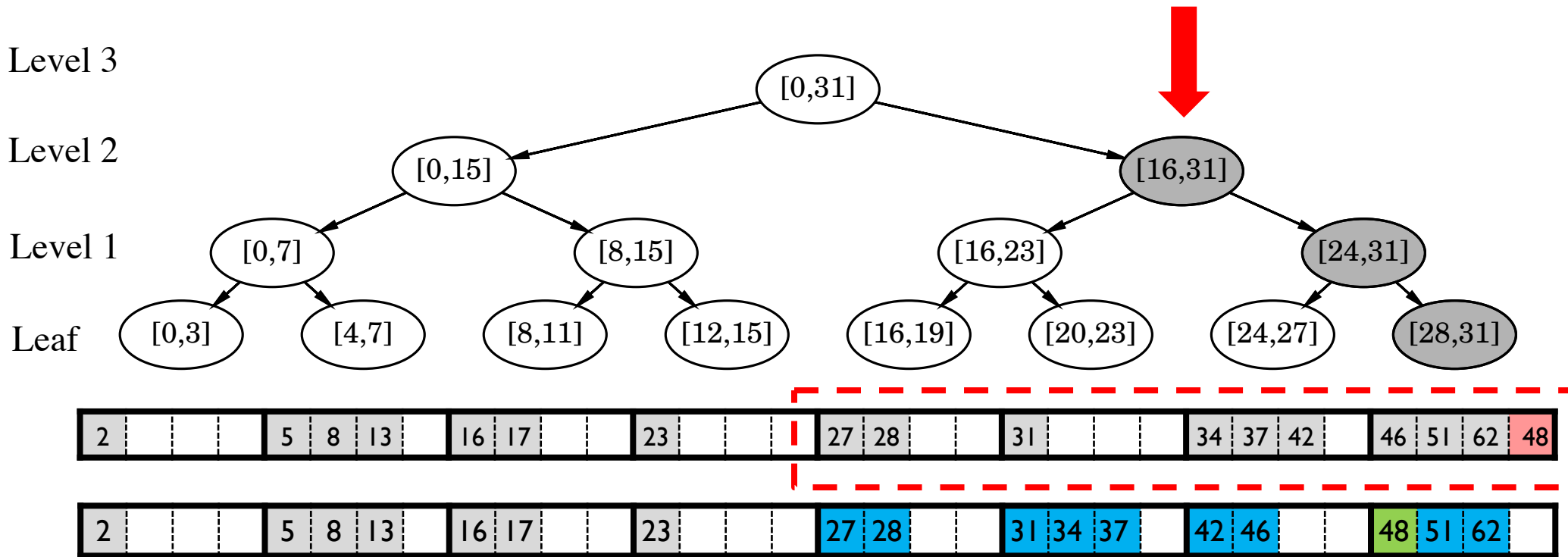
|                            | Leaf | Level 1 | Level 2 | Level 3 |
|----------------------------|------|---------|---------|---------|
| segment size               | 4    | 8       | 16      | 32      |
| density lower bound $\rho$ | 0.08 | 0.19    | 0.29    | 0.40    |
| density upper bound $\tau$ | 0.92 | 0.88    | 0.84    | 0.80    |
| min # of entries           | 1    | 2       | 4       | 8       |
| max # of entries           | 3    | 6       | 12      | 24      |



- [1] Bender, M. A., Demaine, E. D., & Farach-Colton, M. Cache-oblivious b-trees. *SIAM J. Comput.*, 35(2):341–358, 2005.  
 [2] M. A. Bender and H. Hu. An adaptive packed-memory array. *ACM Trans. Database Syst.*, 32(4), 2007.

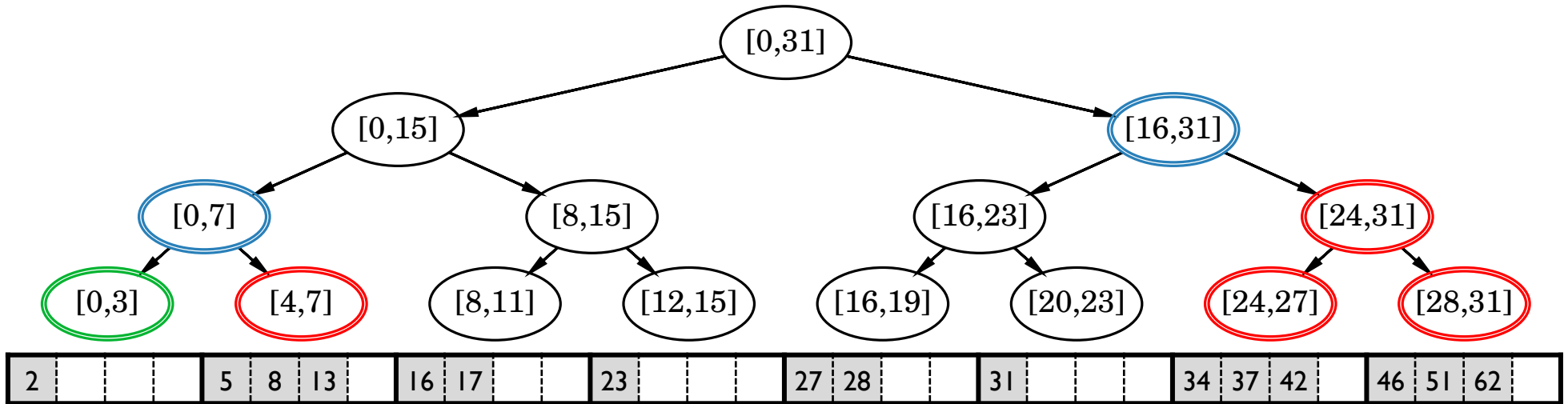
# GPMA Dynamic Graph Processing

|                            | Leaf | Level 1 | Level 2 | Level 3 |
|----------------------------|------|---------|---------|---------|
| segment size               | 4    | 8       | 16      | 32      |
| density lower bound $\rho$ | 0.08 | 0.19    | 0.29    | 0.40    |
| density upper bound $\tau$ | 0.92 | 0.88    | 0.84    | 0.80    |
| min # of entries           | 1    | 2       | 4       | 8       |
| max # of entries           | 3    | 6       | 12      | 24      |

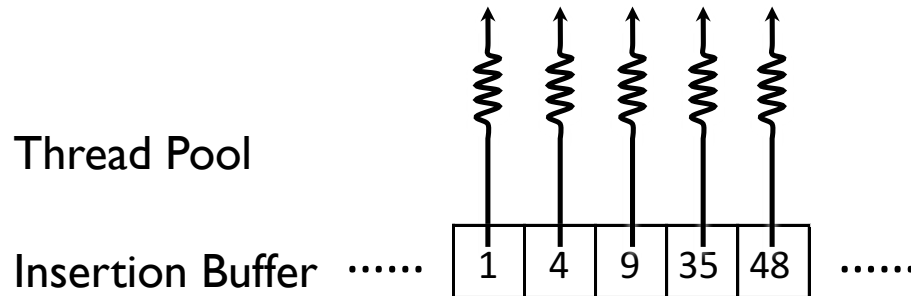
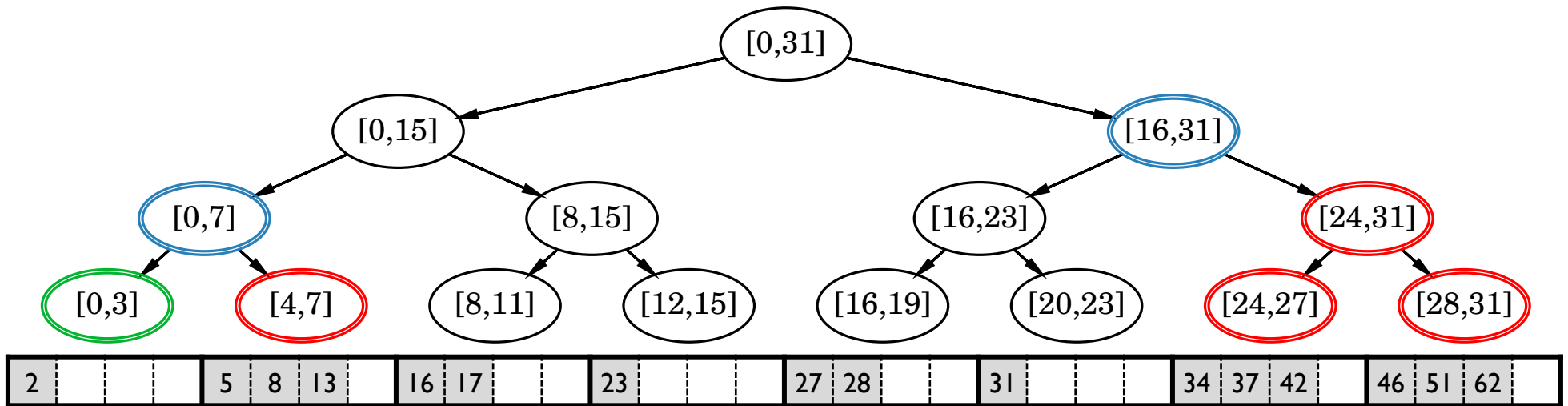


[1] Bender, M. A., Demaine, E. D., & Farach-Colton, M. Cache-oblivious b-trees. *SIAM J. Comput.*, 35(2):341–358, 2005.  
 [2] M. A. Bender and H. Hu. An adaptive packed-memory array. *ACM Trans. Database Syst.*, 32(4), 2007.

# GPMA Dynamic Graph Processing

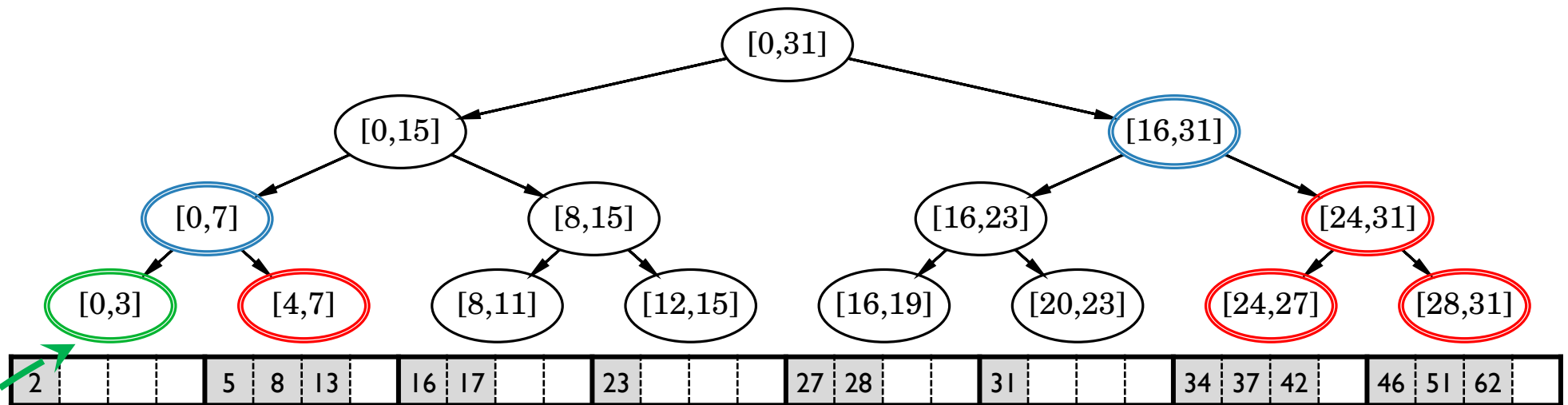


# GPMA Dynamic Graph Processing



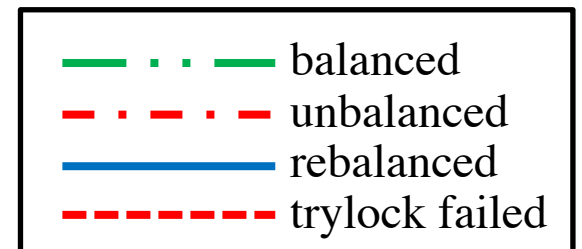


# GPMA Dynamic Graph Processing

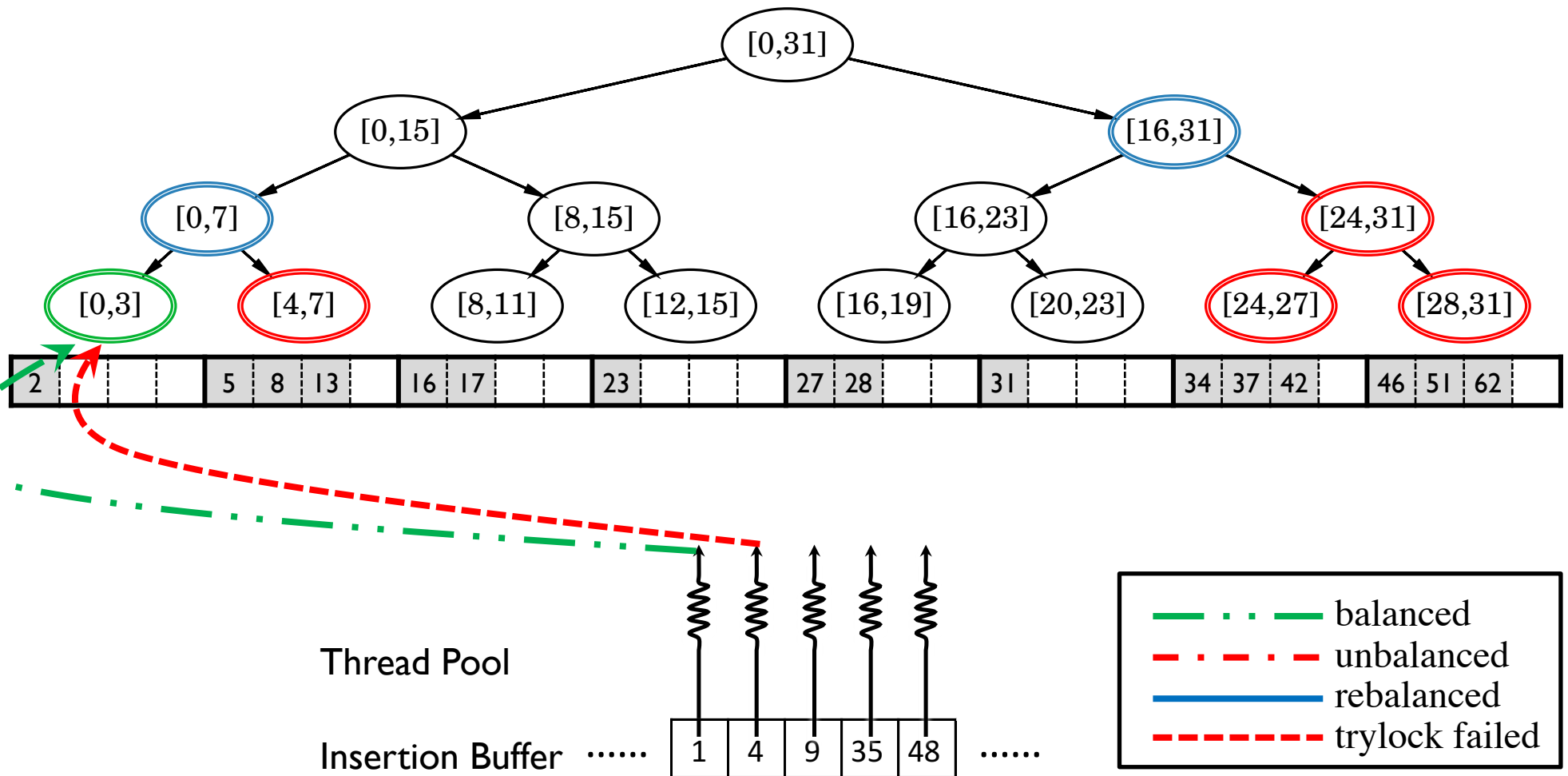


Thread Pool

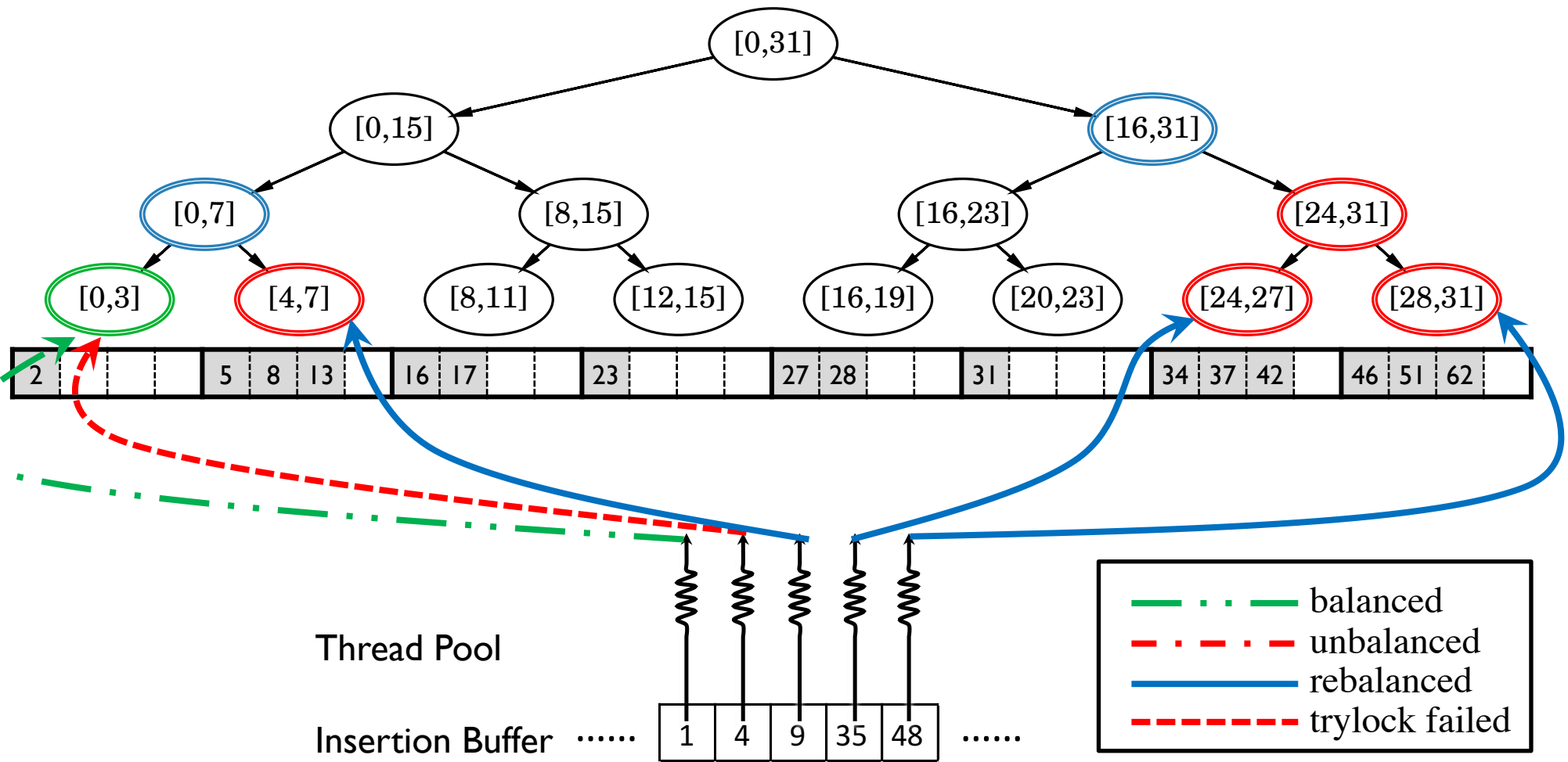
Insertion Buffer ..... 1 4 9 35 48 .....



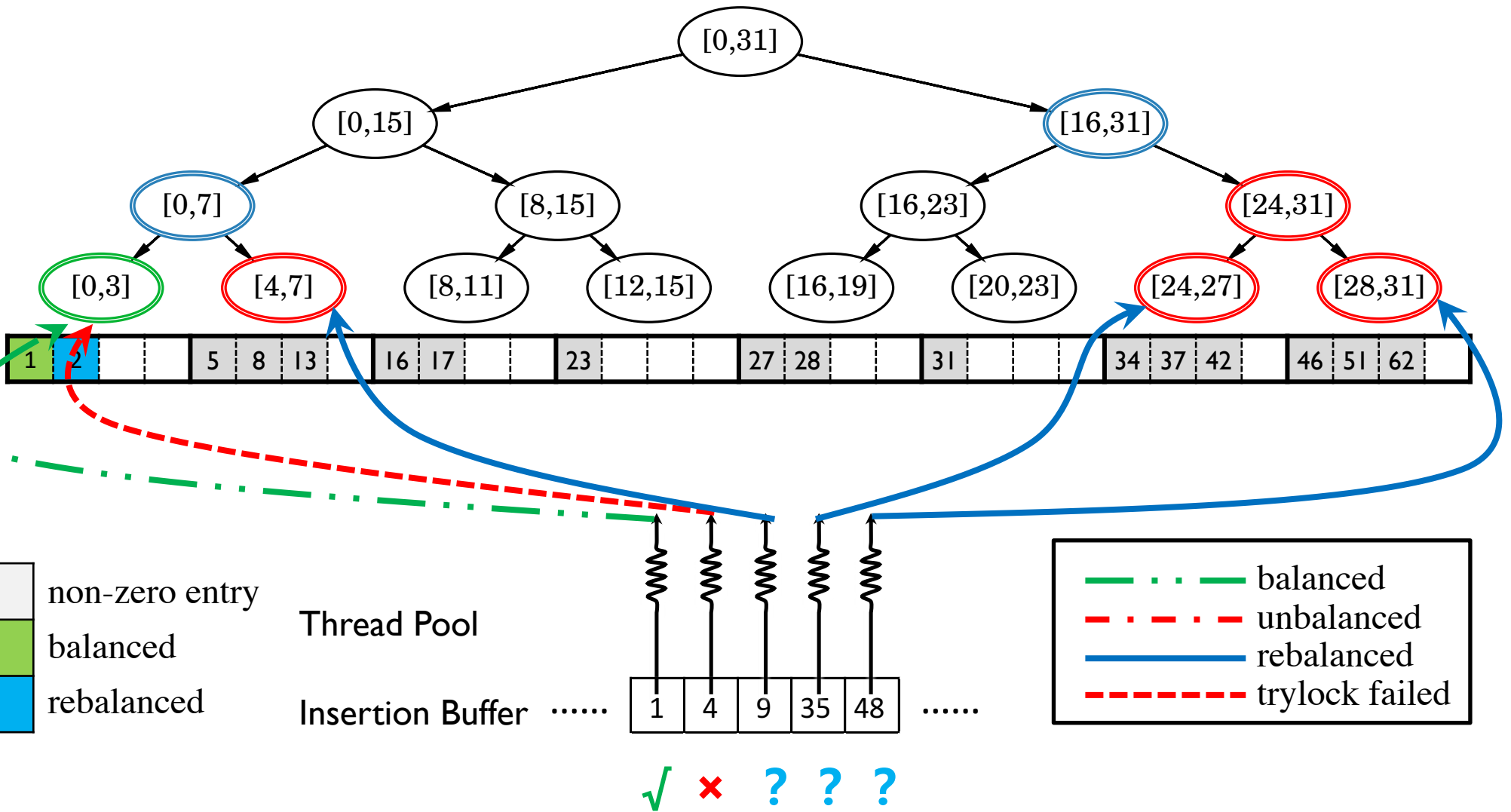
# GPMA Dynamic Graph Processing



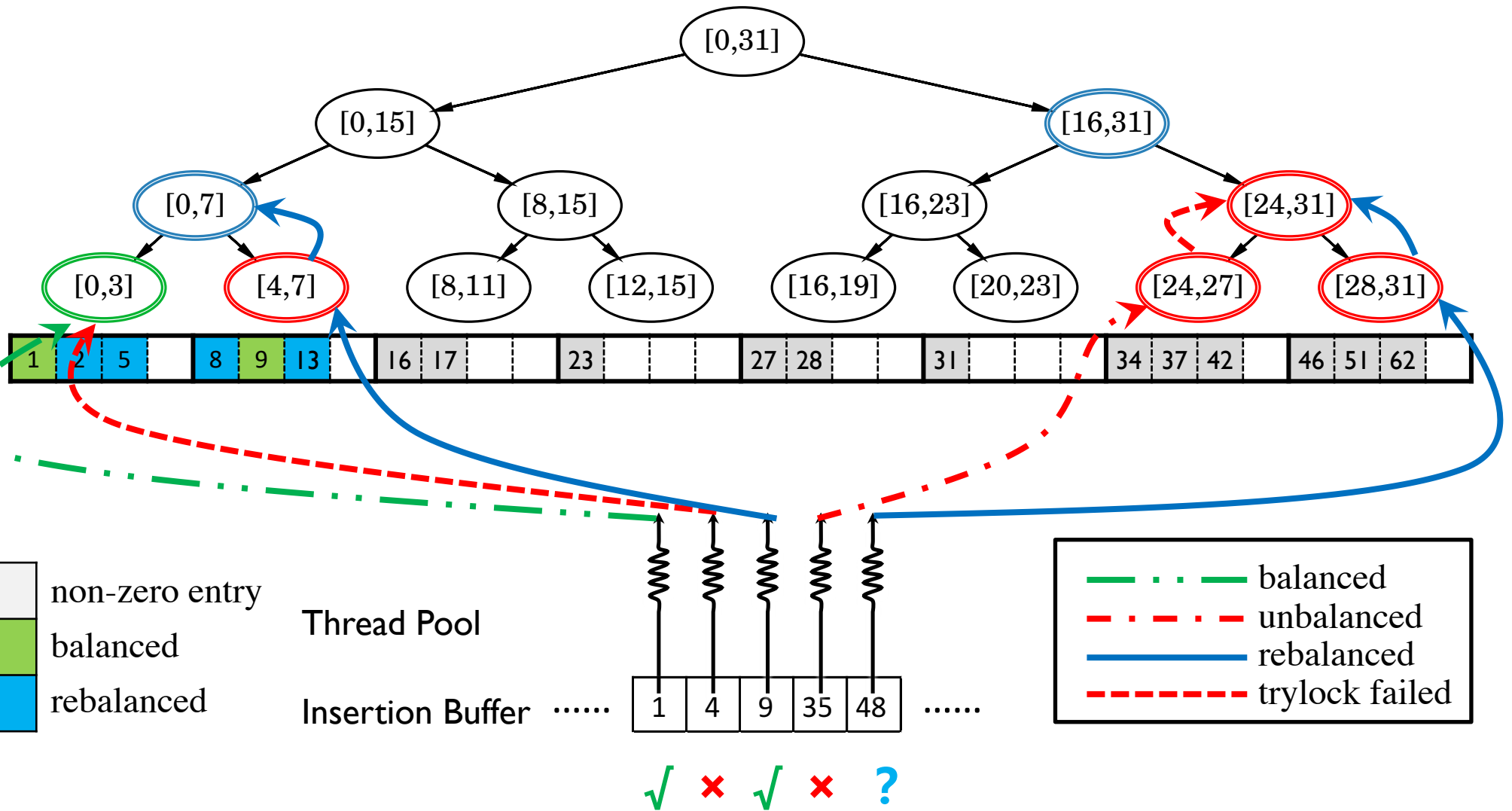
# GPMA Dynamic Graph Processing



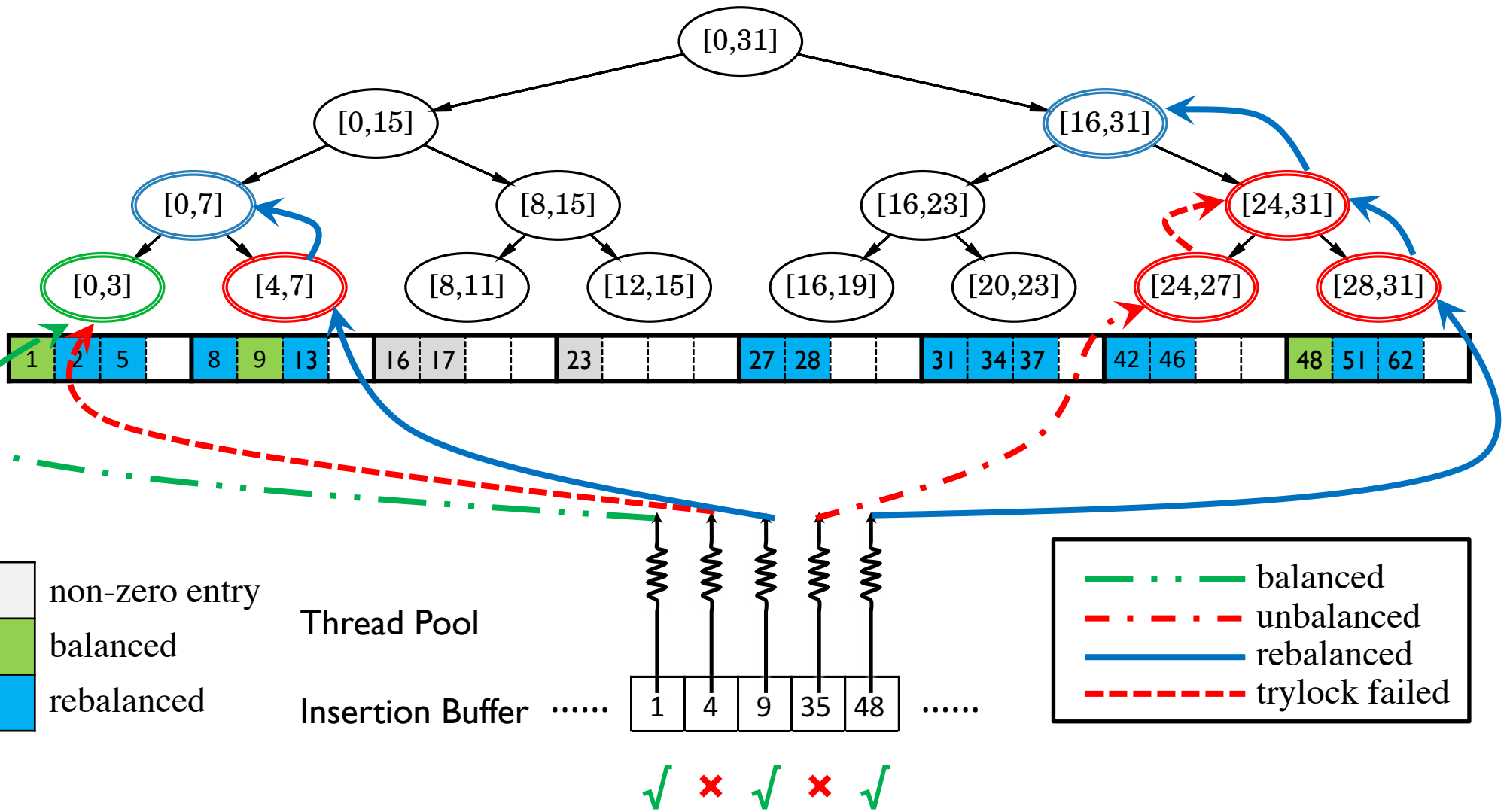
# GPMA Dynamic Graph Processing



# GPMA Dynamic Graph Processing



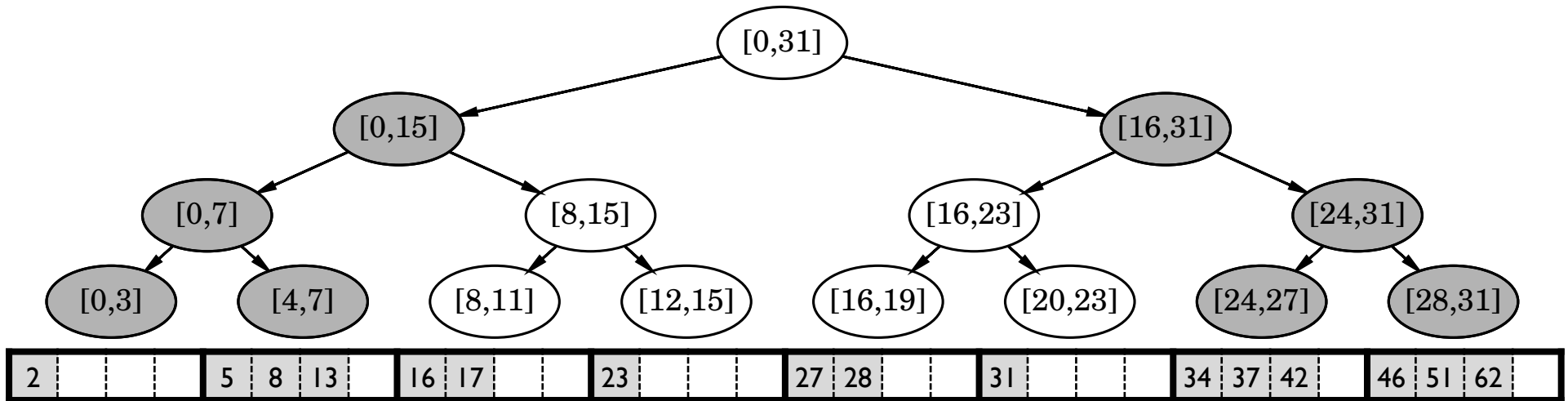
# GPMA Dynamic Graph Processing



# Outline

- Introduction
- **GPMA Dynamic Graph Processing**
- **GPMA+ Optimization**
- Evaluation
- Conclusion

# GPMA+ Optimization

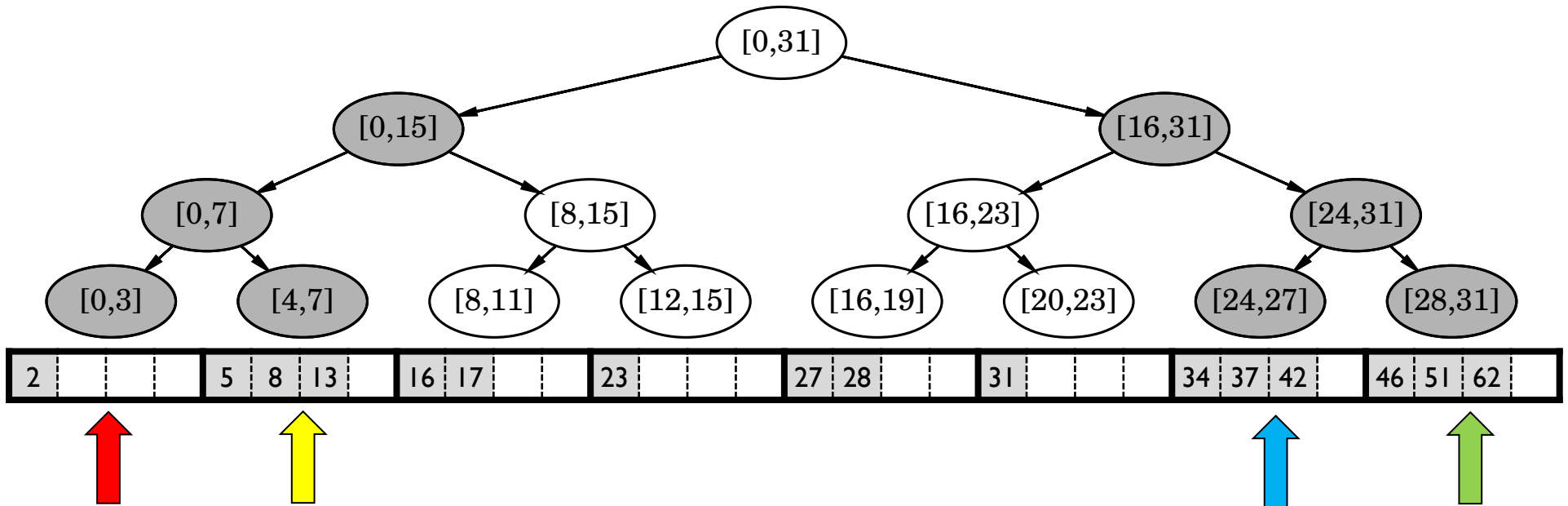


Insertion Keys:

|   |   |   |    |    |
|---|---|---|----|----|
| 1 | 4 | 9 | 35 | 48 |
|---|---|---|----|----|



# GPMA+ Optimization



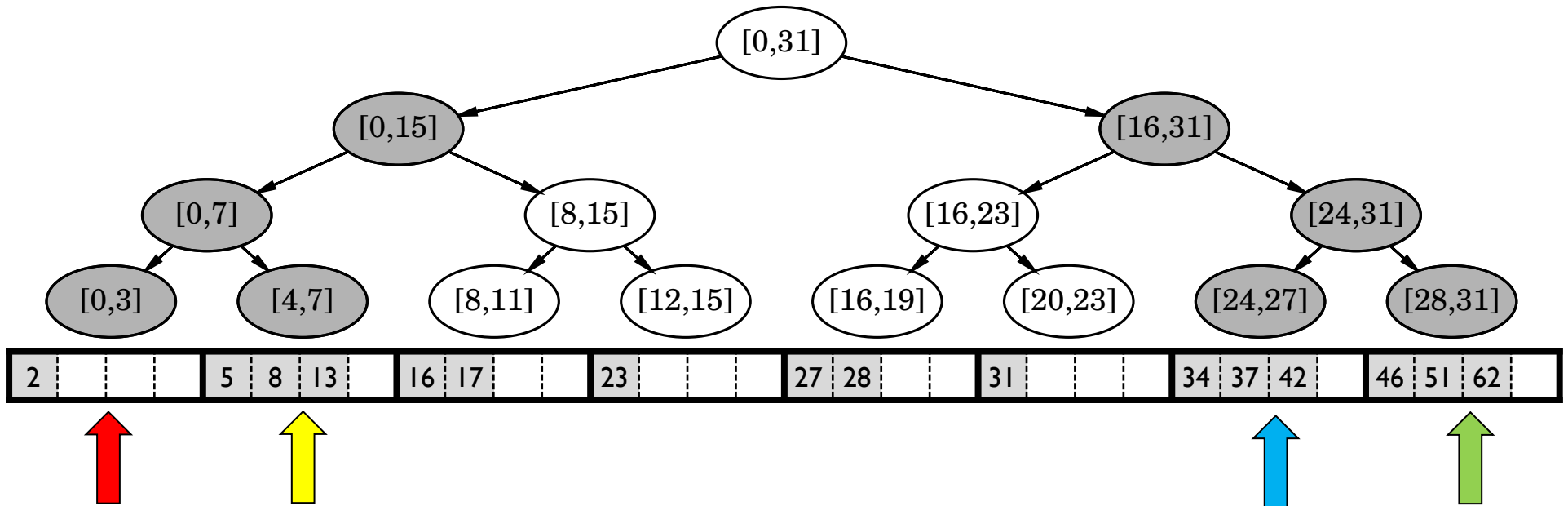
Insertion Keys:

|   |   |   |    |    |
|---|---|---|----|----|
| 1 | 4 | 9 | 35 | 48 |
|---|---|---|----|----|

Leaf Segments:

|   |   |   |    |    |
|---|---|---|----|----|
| 0 | 0 | 4 | 24 | 28 |
|---|---|---|----|----|

# GPMA+ Optimization



Insertion Keys:

|   |   |   |    |    |
|---|---|---|----|----|
| 1 | 4 | 9 | 35 | 48 |
|---|---|---|----|----|

Leaf Segments:

|   |   |   |    |    |
|---|---|---|----|----|
| 0 | 0 | 4 | 24 | 28 |
|---|---|---|----|----|

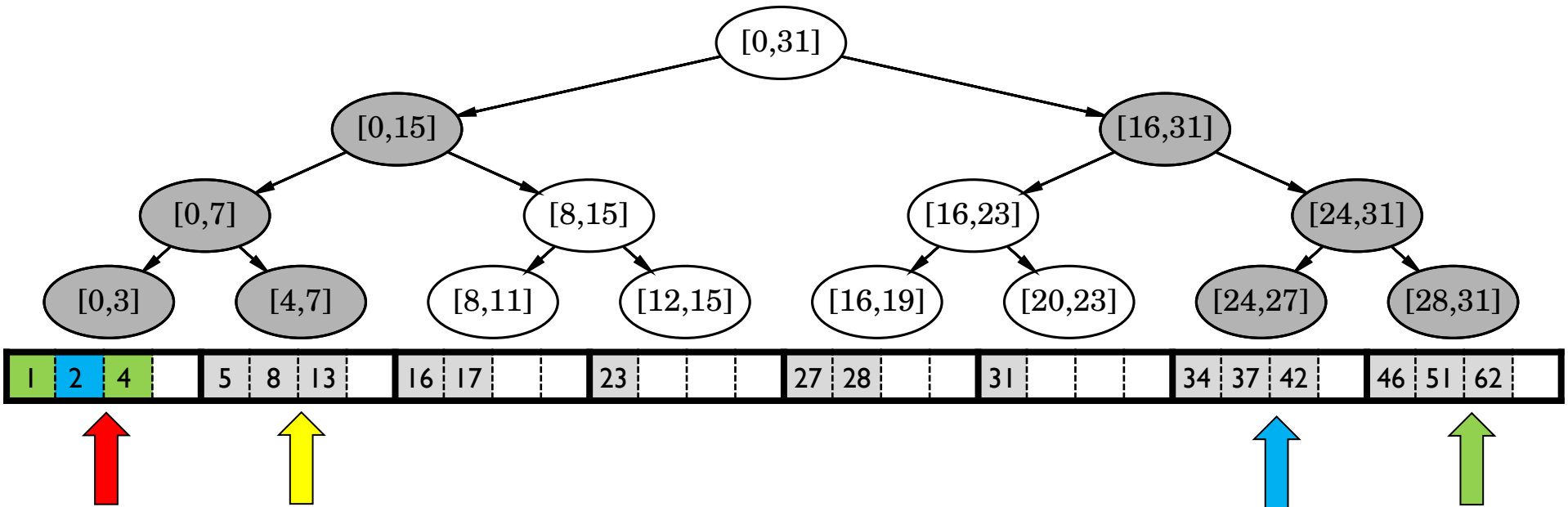
Update Segments:

|   |   |    |    |
|---|---|----|----|
| 0 | 4 | 24 | 28 |
|---|---|----|----|

Update Offsets:

|   |   |   |   |
|---|---|---|---|
| 2 | 3 | 4 | 5 |
|---|---|---|---|

# GPMA+ Optimization



Insertion Keys:

|   |   |   |    |    |
|---|---|---|----|----|
| 1 | 4 | 9 | 35 | 48 |
|---|---|---|----|----|

Leaf Segments:

|   |   |   |    |    |
|---|---|---|----|----|
| 0 | 0 | 4 | 24 | 28 |
|---|---|---|----|----|

Update Segments:

|   |   |    |    |
|---|---|----|----|
| 0 | 4 | 24 | 28 |
|---|---|----|----|

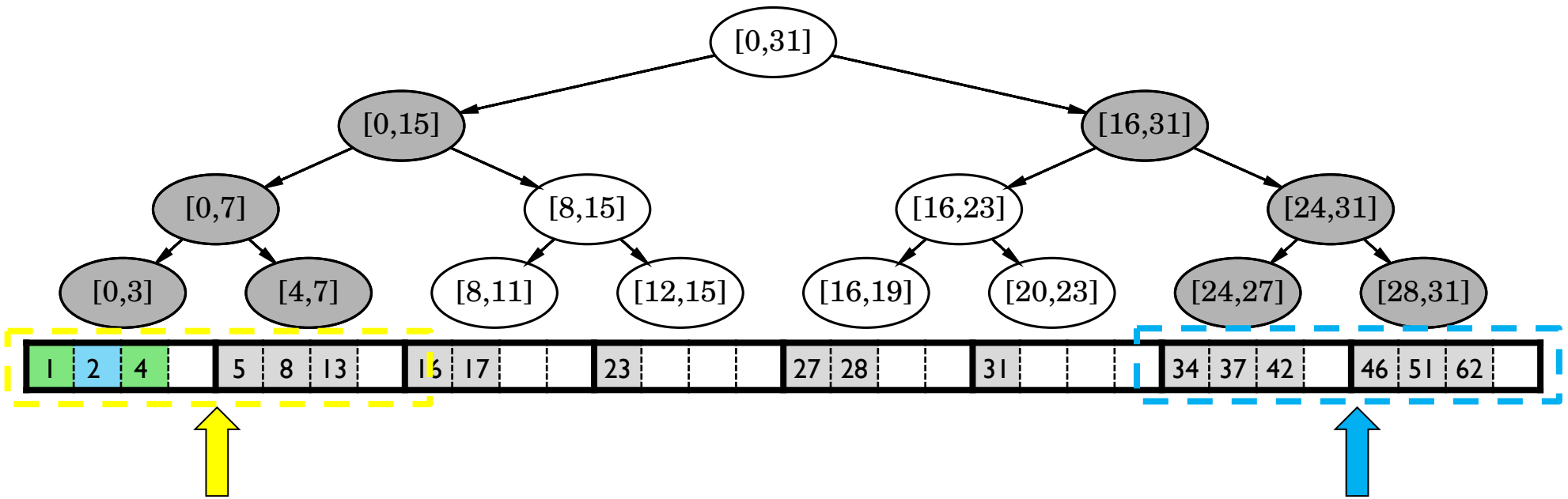
Update Offsets:

|   |   |   |   |
|---|---|---|---|
| 2 | 3 | 4 | 5 |
|---|---|---|---|

Successful Flag:

|   |   |   |   |
|---|---|---|---|
| Y | N | N | N |
|---|---|---|---|

# GPMA+ Optimization



Insertion Keys: 

|   |   |   |    |    |
|---|---|---|----|----|
| 1 | 4 | 9 | 35 | 48 |
|---|---|---|----|----|

Leaf Segments: 

|   |   |   |    |    |
|---|---|---|----|----|
| 0 | 0 | 4 | 24 | 28 |
|---|---|---|----|----|

Update Segments: 

|   |   |    |    |
|---|---|----|----|
| 0 | 4 | 24 | 28 |
|---|---|----|----|

Update Offsets: 

|   |   |   |   |
|---|---|---|---|
| 2 | 3 | 4 | 5 |
|---|---|---|---|

Successful Flag: 

|   |   |   |   |
|---|---|---|---|
| Y | N | N | N |
|---|---|---|---|

Insertion Keys: 

|   |    |    |
|---|----|----|
| 9 | 35 | 48 |
|---|----|----|

Update Segments: 

|   |    |
|---|----|
| 0 | 24 |
|---|----|

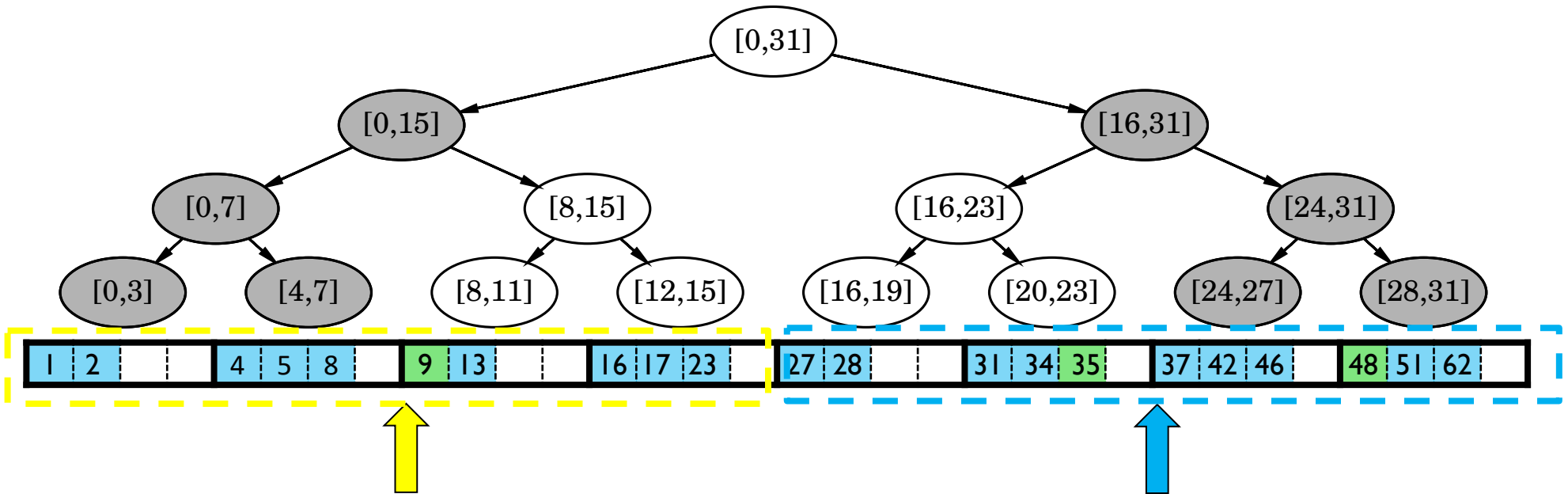
Update Offsets: 

|   |   |
|---|---|
| 1 | 3 |
|---|---|

Successful Flag: 

|   |   |
|---|---|
| N | N |
|---|---|

# GPMA+ Optimization



Insertion Keys: 

|   |   |   |    |    |
|---|---|---|----|----|
| 1 | 4 | 9 | 35 | 48 |
|---|---|---|----|----|

Leaf Segments: 

|   |   |   |    |    |
|---|---|---|----|----|
| 0 | 0 | 4 | 24 | 28 |
|---|---|---|----|----|

Update Segments: 

|   |   |    |    |
|---|---|----|----|
| 0 | 4 | 24 | 28 |
|---|---|----|----|

Update Offsets: 

|   |   |   |   |
|---|---|---|---|
| 2 | 3 | 4 | 5 |
|---|---|---|---|

Successful Flag: 

|   |   |   |   |
|---|---|---|---|
| Y | N | N | N |
|---|---|---|---|

Insertion Keys: 

|   |    |    |
|---|----|----|
| 9 | 35 | 48 |
|---|----|----|

Update Segments: 

|   |    |
|---|----|
| 0 | 24 |
|---|----|

Update Offsets: 

|   |   |
|---|---|
| 1 | 3 |
|---|---|

Successful Flag: 

|   |   |
|---|---|
| N | N |
|---|---|

Insertion Keys: 

|   |    |    |
|---|----|----|
| 9 | 35 | 48 |
|---|----|----|

Update Segments: 

|   |    |
|---|----|
| 0 | 16 |
|---|----|

Update Offsets: 

|   |   |
|---|---|
| 1 | 3 |
|---|---|

Successful Flag: 

|   |   |
|---|---|
| Y | Y |
|---|---|

# Outline

- Introduction
- **GPMA Dynamic Graph Processing**
- **GPMA+ Optimization**
- **Evaluation**
- Conclusion

# Evaluation

## Datasets

|          | V     | E     |
|----------|-------|-------|
| Reddit   | 2.61M | 34.4M |
| Pokec    | 1.6M  | 30.6M |
| Graph500 | 1M    | 200M  |
| Random   | 1M    | 200M  |

## Baselines

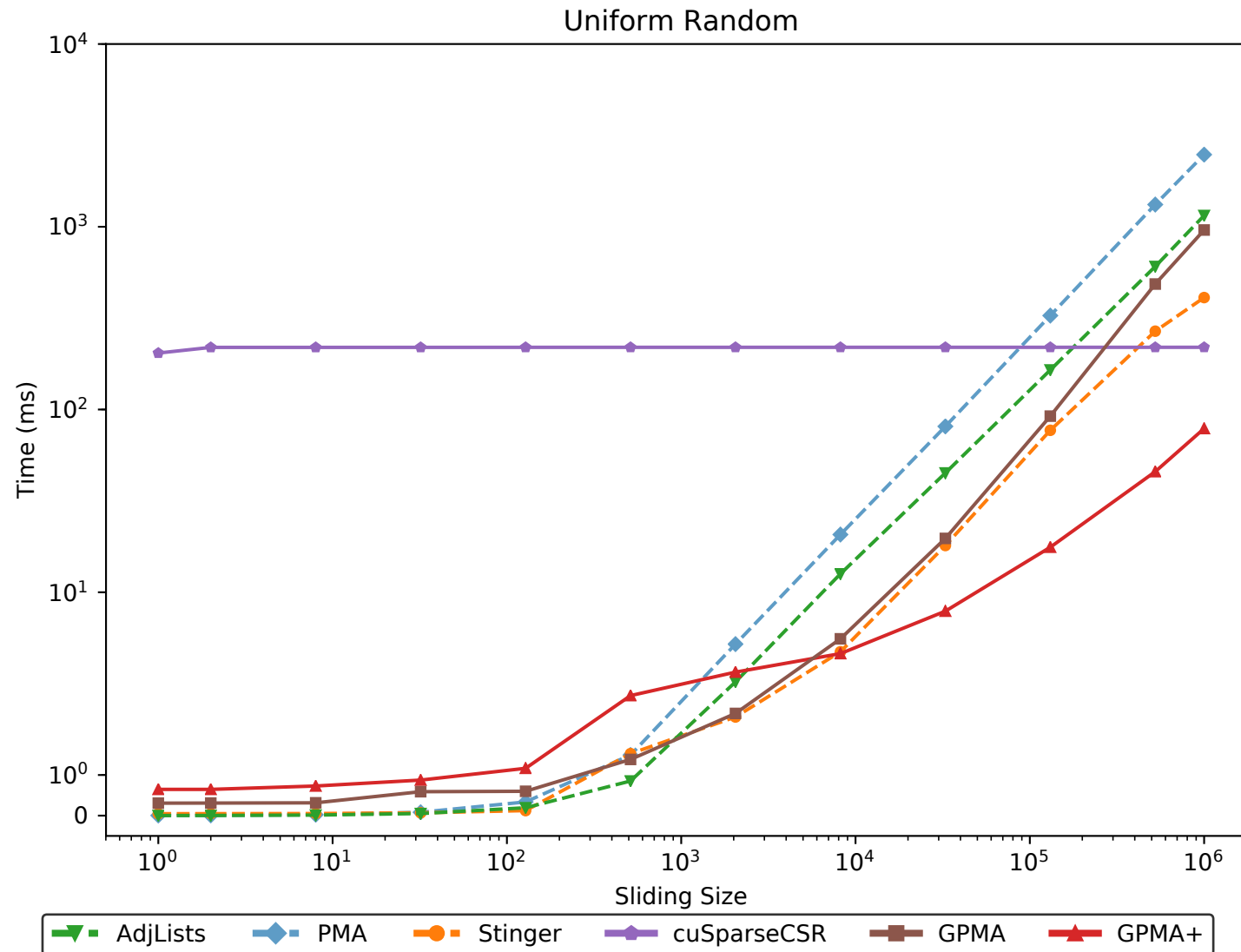
|                   | Container   | BFS                                  | Connect<br>Component | PageRank  |
|-------------------|-------------|--------------------------------------|----------------------|-----------|
| CPU<br>Approaches | AdjLists    | Standard Single Thread Algorithms    |                      |           |
|                   | PMA         |                                      |                      |           |
|                   | Stinger     | Stinger built-in Parallel Algorithms |                      |           |
| GPU<br>Approaches | cuSparseCSR | D. Merrill et al.                    | J. Soman et al.      | CUSP SpMV |
|                   | GPMA+       |                                      |                      |           |

## Specification

- CPU-based  
4-way Intel(R) Xeon(R) CPU E7-4820 v3  
40-cores, 1.90GHz  
128GB memory
- GPU-based  
Intel(R) Core i7-5820k  
6-cores, 3.30GHz  
64GB memory  
Nvidia GeForce Titan X 12GB

# Evaluation

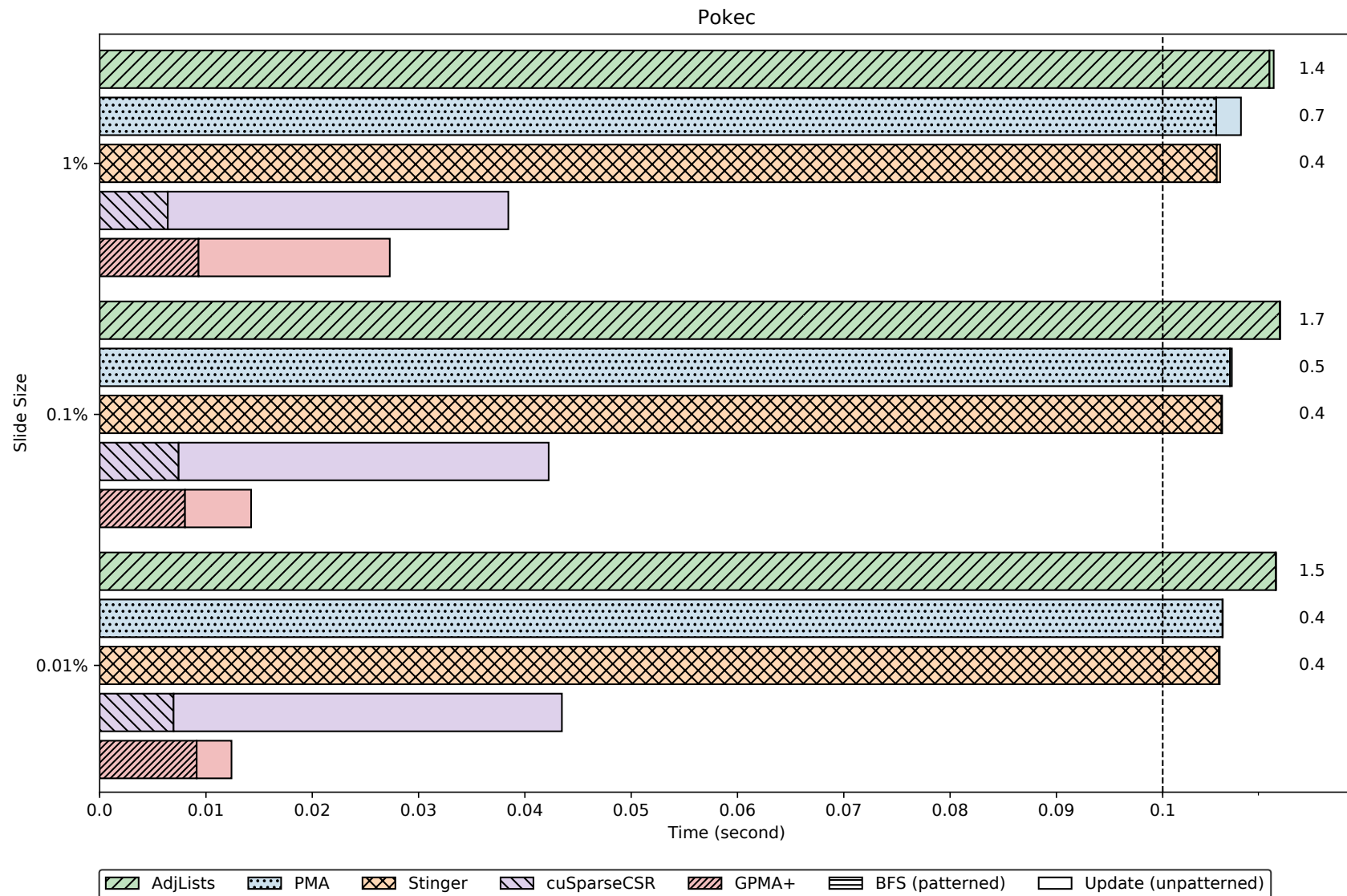
## Insertion





# Evaluation

## BFS



# Outline

- Introduction
- **GPMA Dynamic Graph Processing**
- **GPMA+ Optimization**
- Evaluation
- **Conclusion**

# Conclusion

- I. ***We introduce a framework for GPU dynamic graph analytics and propose, the first of its kind, a GPU dynamic graph storage scheme to pave the way for real-time dynamic graph analytics on GPUs.***
  
- II. ***We devise two GPU-oriented parallel algorithms: GPMA and GPMA+, to support efficient updates against high-speed graph streams.***
  
- III. ***We conduct extensive experiments to show the performance superiority of GPMA and GPMA+.***

**Thank you!**



Open Source: [https://github.com/desert0616/gpma\\_bfs\\_demo](https://github.com/desert0616/gpma_bfs_demo)